



Hash functions

From CRC to SHA-2

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First look

Properties:

- Low cost
- Determinism
- Uniformity
- One-way - difficult to find data for given hash
- Collision resistance - difficult to find $x \neq y; \varphi(x) = \varphi(y)$
- Infeasible to modify data without changing hash



CRC - Cyclic redundancy check

$$\begin{array}{r|l} M(x) = & 100101_2 = x^5 + x^2 + 1 \\ G(x) = & \text{XOR } 110011_2 = x^5 + x^4 + x + 1 \\ \hline R(x) = & 010110_2 = x^4 + x^2 + x \end{array}$$



Whirlpool and Tiger

	<i>Whirlpool</i>	<i>Tiger</i>
<i>Designed</i>	2000	1996
<i>Hash size</i>	512b	192b
– <i>string</i>	128B	48B
<i>Attacks</i>	<i>Coll. in 2^{120}</i>	<i>not known</i>



MD5 - Message digest version 5

Hash length = 128b (32B in human readable string)

- 1991, Donald Rivest, MIT
- 1993, pseudo-collision
- 1996, first particular collision
- 2004, birthday attack
- 2004, full collision
- 2005, two X.509 certificates with the same hash
- 2005, Vlastimil Klíma, alg. to find collision in one minute
- 2010, single-block collision, secret algorithm

Vlastimil Klíma - most efficient MD5 collision algorithm



SHA1 - Secure hash algorithm version 1

Hash length = 160b (40B in human readable string)

- 1995, NSA
- 2005, collision in 2^{69} operations (strong is 2^{80})
- 2007, collision in 2^{63} operations
- 2007, began distributed collisions (BOINC)
- 2008, Stéphane Manuel - theoretic collision in $2^{51} - 2^{57}$
- 2010, full attack in $2^{57.5}$ operations



SHA2 - Secure hash algorithm version 2

Family of algorithms (SHA-224, SHA-256, SHA-384, SHA-512)

No collisions found

	<i>SHA – 224/256</i>	<i>SHA – 384/512</i>
<i>Hash size</i>	224/256b	384/512b
<i>– string</i>	56/64B	96/128B
<i>Max input</i>	$2^{64} - 1b$	$2^{128} - 1b$



How we can find collision?

$$\varphi(x) = ed076287532e86365e841e92bfc50d8c$$

- Google it
- Rainbow tables
- Social engineering
- Bruteforce algorithms:
 - Dark room
 - Computer power



And how make hash stronger?

- Combine functions from different families
- Salt data
- Truncate hash to lower length (carefully)

$MD5 \leftarrow SHA1 \leftarrow Tiger \leftarrow SHA2 \leftarrow Whirlpool$

$32 \leftarrow 40 \leftarrow 48 \leftarrow 56/64/96/128 \leftarrow 128$

- Freely combine methods above



Further reading

`fjfi.lainspira.net/ukry/hash_functions.pdf`

- `cryptography.hyperlink.cz/`
- `en.wikipedia.org/wiki/MD5`
- `en.wikipedia.org/wiki/SHA-1`
- `en.wikipedia.org/wiki/SHA-2`
- `en.wikipedia.org/wiki/Whirlpool_%28cryptography%29`
- `en.wikipedia.org/wiki/Tiger_%28cryptography%29`
- `en.wikipedia.org/wiki/Crypt_%28Unix%29#Library_Function`